

Università degli Studi di Padova – Dipartimento di Ingegneria Industriale

Corso di Laurea in Ingegneria Meccanica

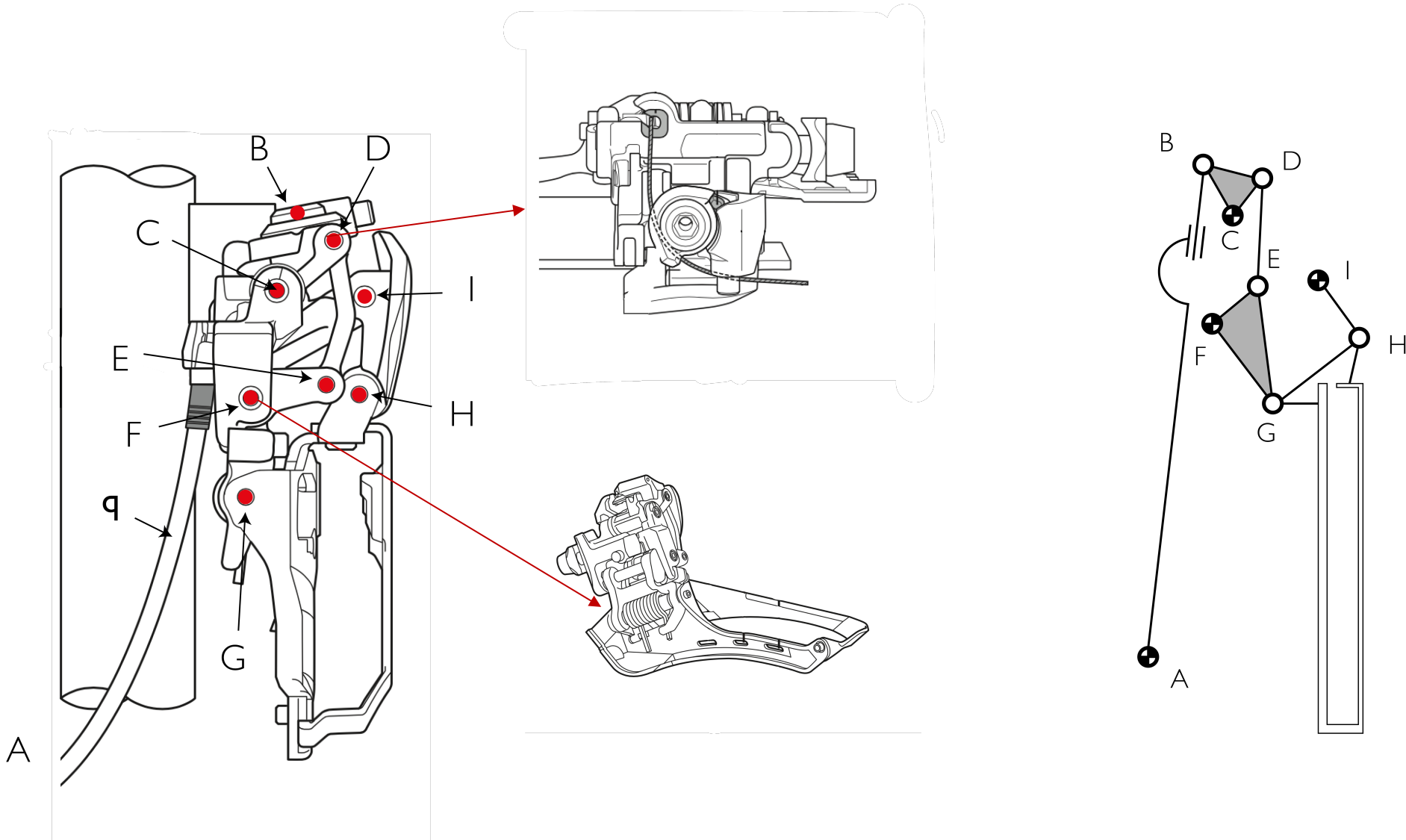
***Relazione per la prova finale  
«Analisi cinematica del deragliatore  
anteriore del gruppo Shimano 105»***

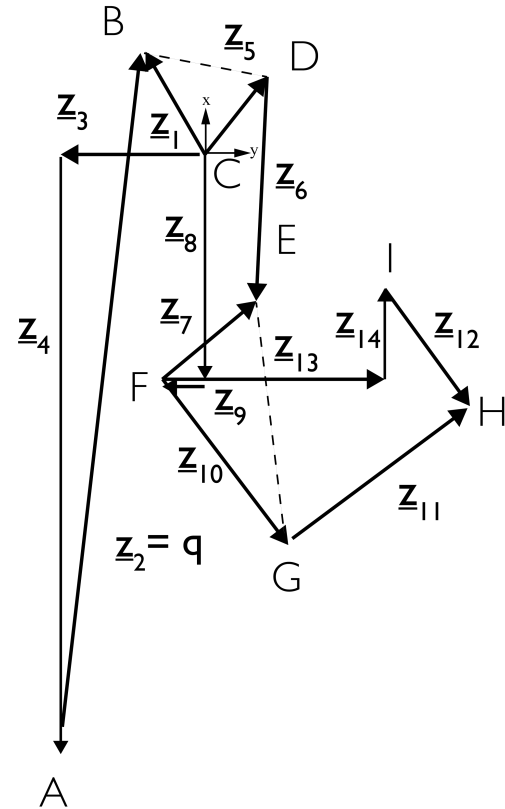
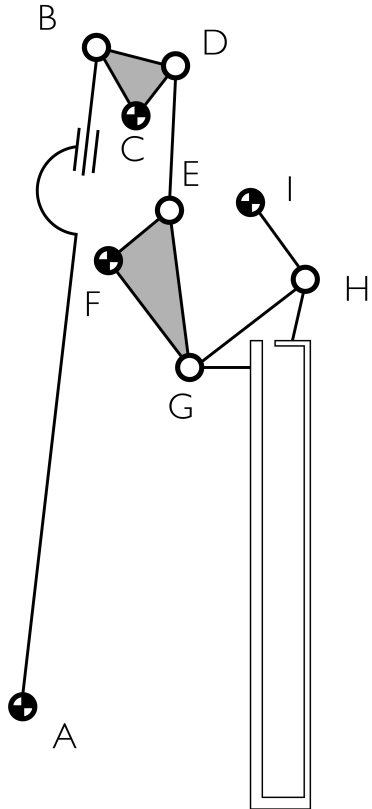
Tutor universitario: Prof. Giulio Rosati

Laureando: *Filippo Russo*

Padova, 9/03/2022







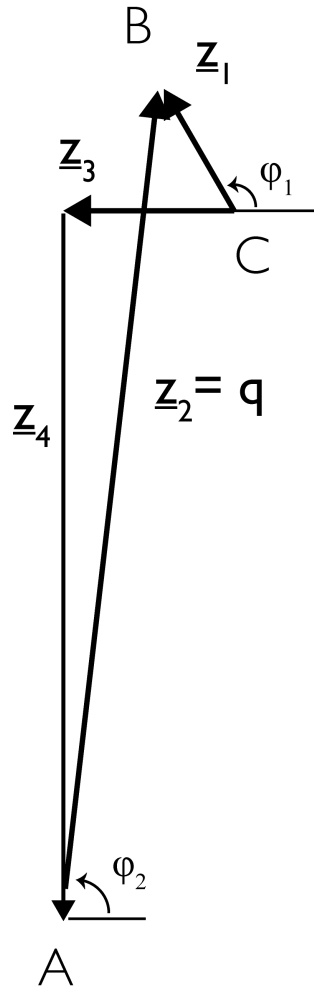
## MAGLIE DEL MECCANISMO

$$\underline{z}_2 - \underline{z}_1 + \underline{z}_3 + \underline{z}_4 = \underline{0}$$

$$\underline{z}_5 + \underline{z}_6 - \underline{z}_7 - \underline{z}_8 - \underline{z}_9 = \underline{0}$$

$$\underline{z}_{13} + \underline{z}_{14} + \underline{z}_{12} - \underline{z}_{11} - \underline{z}_{10} = \underline{0}$$

VARIABILI  $q, \varphi_1, \varphi_2, \varphi_5, \varphi_6, \varphi_7, \varphi_{10}, \varphi_{11}, \varphi_{12}$



$$\underline{z_2} - \underline{z_1} + \underline{z_3} + \underline{z_4} = \underline{0}$$

$$q \begin{Bmatrix} \cos \varphi_2 \\ \sin \varphi_2 \end{Bmatrix} - a_1 \begin{Bmatrix} \cos \varphi_1 \\ \sin \varphi_1 \end{Bmatrix} + a_3 \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} + a_4 \begin{Bmatrix} 0 \\ 1 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \end{Bmatrix}$$

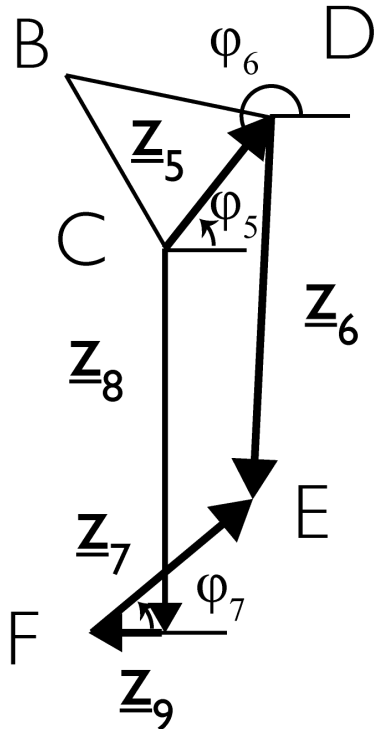
$$L_{AC} = \sqrt{x_A^2 + y_A^2}$$

$$\varphi_2 = \left( \sin^{-1} \left( \frac{-x_A}{L_{CA}} \right) + \cos^{-1} \left( \frac{q^2 + (L_{AC})^2 - a_1^2}{2qL_{AC}} \right) \right)$$

$$x_B = x_A + q \cos \varphi_2$$

$$y_B = y_A + q \sin \varphi_2$$

$$\varphi_1 = \pi - \cos^{-1} \left( \frac{-x_B}{a_1} \right)$$



$$\underline{z}_5 + \underline{z}_6 - \underline{z}_7 - \underline{z}_8 - \underline{z}_9 = \underline{0}$$

$$a_5 \begin{Bmatrix} \cos \varphi_5 \\ \sin \varphi_5 \end{Bmatrix} + a_6 \begin{Bmatrix} \cos \varphi_6 \\ \sin \varphi_6 \end{Bmatrix} - a_7 \begin{Bmatrix} \cos \varphi_7 \\ \sin \varphi_7 \end{Bmatrix} - a_8 \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} - a_9 \begin{Bmatrix} 0 \\ 1 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \end{Bmatrix}$$

$$\varphi_5 = \varphi_1 - \cos^{-1} \left( \frac{a_1^2 + a_5^2 - L_{BD}^2}{2 a_1 a_5} \right)$$

$$x_D = a_5 \cos \varphi_5$$

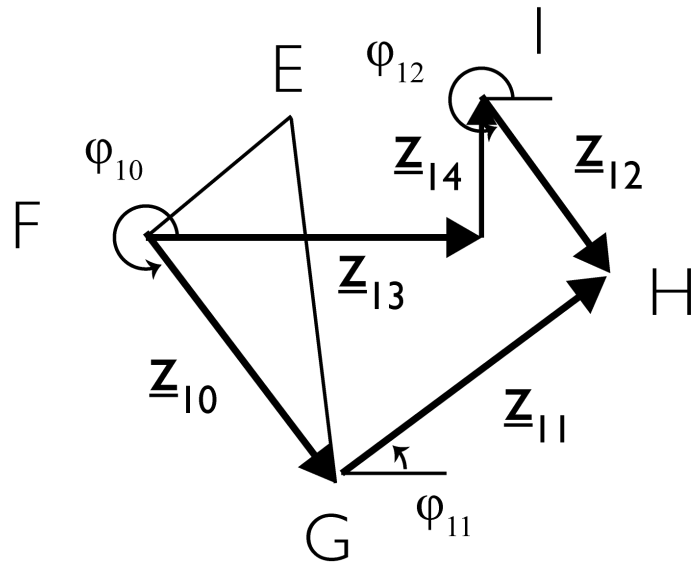
$$y_D = a_5 \sin \varphi_5$$

$$\varphi_6 = \pi + \cos^{-1} \left( \frac{(x_D - x_F)}{(L_{FD})} \right) + \cos^{-1} \left( \frac{(a_6^2 + L_{FD}^2 - a_7^2)}{2 a_6 L_{FD}} \right)$$

$$x_E = x_D + a_6 \cos \varphi_6$$

$$y_E = y_D + a_6 \sin \varphi_6$$

$$\varphi_7 = \cos^{-1} \left( \frac{x_E - x_F}{a_7} \right)$$



$$\underline{z}_{10} + \underline{z}_{11} - \underline{z}_{12} - \underline{z}_{14} - \underline{z}_{13} = \underline{0}$$

$$a_{13} \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} + a_{14} \begin{Bmatrix} 0 \\ 1 \end{Bmatrix} + a_{12} \begin{Bmatrix} \cos \varphi_{12} \\ \sin \varphi_{12} \end{Bmatrix} - a_{11} \begin{Bmatrix} \cos \varphi_{11} \\ \sin \varphi_{11} \end{Bmatrix} - a_{10} \begin{Bmatrix} \cos \varphi_{10} \\ \sin \varphi_{10} \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \end{Bmatrix}$$

$$\varphi_{10} = \varphi_7 - \cos^{-1} \left( \frac{a_7^2 + a_{10}^2 - L_{GE}^2}{2a_7a_{10}} \right)$$

$$x_G = x_F + a_{10} \cos \varphi_{10}$$

$$y_G = y_F + a_{10} \sin \varphi_{10}$$

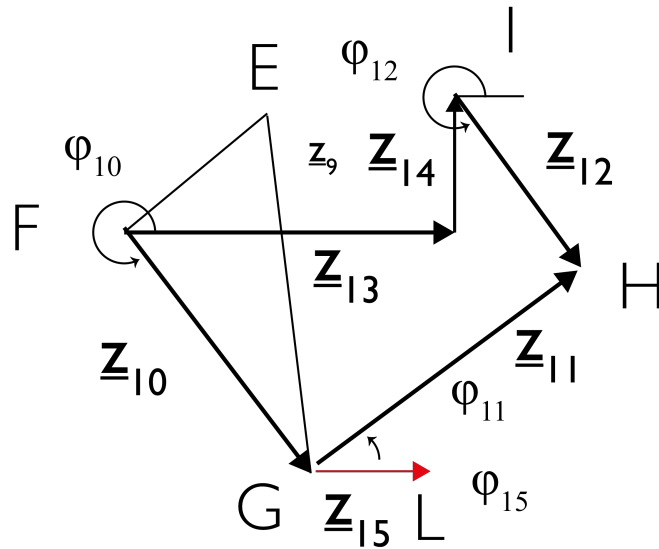
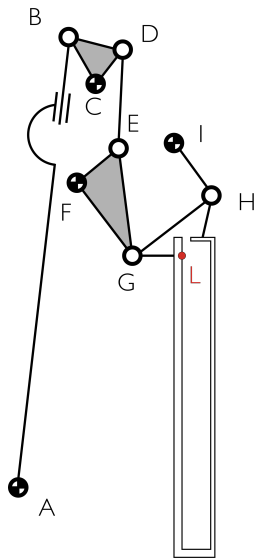
$$L_{GI} = \sqrt{(x_I - x_G)^2 + (y_I - y_G)^2}$$

$$\varphi_{11} = \frac{\pi}{2} - \left[ \cos^{-1} \left( \frac{(x_I - x_G)}{L_{GI}} \right) + \cos^{-1} \left( \frac{L_{GI}^2 + a_{11}^2 - a_{12}^2}{2a_{11}L_{GI}} \right) \right]$$

$$x_H = x_G + a_{11} \cos \varphi_{11}$$

$$y_H = y_G + a_{11} \sin \varphi_{11}$$

$$\varphi_{12} = \frac{3}{2}\pi + \sin^{-1} \left( \frac{x_H - x_I}{a_{12}} \right)$$



## PUNTO L

$$\mathbf{x}_L = x_F + a_{10} \cos \varphi_{10} + L_{GL} \cos \varphi_{15}$$

$$\varphi_{15} = \varphi_{11} - H\hat{G}M$$

$$\dot{x}_L = -a_{10} \sin \varphi_{10} \dot{\varphi}_{10} - L_{GL} \sin \varphi_{15} \dot{\varphi}_{11}$$

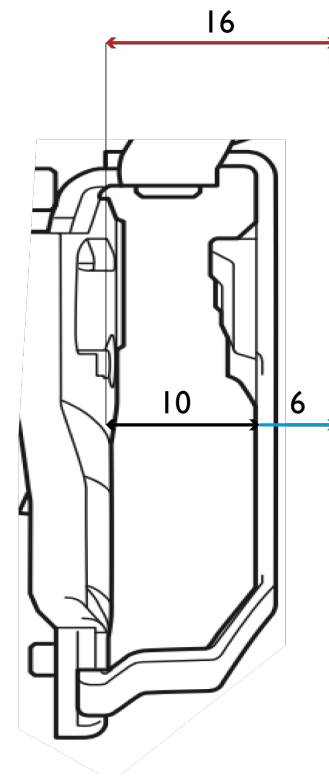
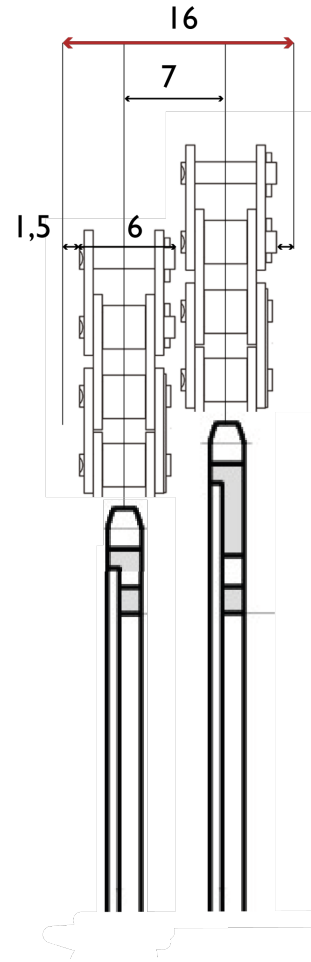
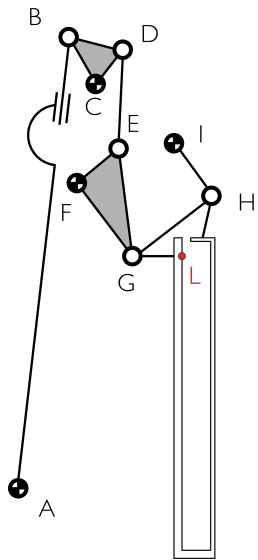
$$W_{x_L} = \frac{\dot{x}_L}{\dot{q}} = -a_{10} \sin \varphi_{10} W_{\varphi_{10}} - L_{GL} \sin \varphi_{15} W_{\varphi_{11}}$$

$$W_{\varphi_{11}} = -\frac{a_{10} \sin(\varphi_{10} - \varphi_{11})}{a_{11} \sin(\varphi_{11} - \varphi_{12})} W_{\varphi_{12}} \quad W_{\varphi_{10}} = W_{\varphi_{12}} = -\frac{a_5 \sin(\varphi_5 - \varphi_6)}{a_7 \sin(\varphi_6 - \varphi_7)} W_{\varphi_5}$$

$$W_{\varphi_5} = W_{\varphi_1} = -\frac{1}{a_1 \sin(\varphi_1 - \varphi_2)}$$

$$\frac{dW_{x_L}}{dq} = \frac{\ddot{x}_L}{\dot{q}^2} = \frac{d}{dq} \left( -a_{10} \sin \varphi_{10} \frac{a_5 \sin(\varphi_5 - \varphi_6)}{a_7 \sin(\varphi_6 - \varphi_7)} \frac{1}{a_1 \sin(\varphi_1 - \varphi_2)} - L_{GL} \sin \varphi_{11} \left( -\frac{a_{10} \sin(\varphi_{10} - \varphi_{11})}{a_{11} \sin(\varphi_{11} - \varphi_{12})} \right) \left( \frac{a_5 \sin(\varphi_5 - \varphi_6)}{a_7 \sin(\varphi_6 - \varphi_7)} \right) \left( \frac{1}{a_1 \sin(\varphi_1 - \varphi_2)} \right) \right)$$





[mm]

